

Applied Laplace- and z-Transforms for Scientists and Engineers

A Computational Approach Using a *Mathematica* Package

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